

CLASSICALIZATION OF THE NON-LINEAR SCHRODINGER EQUATION

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Abstract

The Non-linear Schrodinger Equation (NLSE), (in units of $\hbar = 1$

$$i \frac{\partial \psi}{\partial t} + a \frac{\partial^2 \psi}{\partial x^2} + \beta |\psi|^\rho \psi = 0$$
 where $\rho = 1, 2, 3, \dots, \alpha$ is a positive real constant, and β is a real constant, E is the energy, is known to be integral for infinite X

space. A Fourier analysis in a bounded interval $|X| \leq L$, i.e. $u(x) = \sum_j u_j \exp(ik_j x)$ shows that the NLSE is a nonlinear Hamiltonian system of N degrees of freedom. The effect of truncating the degrees of freedom to a finite number N and the fact that L is finite are investigated for the case $\alpha = +1, \beta = 1$ and $\rho = 2$. The results show that chaos sets in at certain value of the energy as the energy – increases for fixed N. Hence the NLSE is not integrable for finite N, and L. However, the integrability increases with increase in N implying that as N tends to infinity the NLSE becomes completely integrable as expected..